

R09**Code No: 09A30205****JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY, HYDERABAD
B.Tech II Year I Semester Examinations, May/June-2013****Electromagnetic Fields
(Electrical and Electronics Engineering)****Time: 3 hours****Max. Marks: 75****Answer any five questions
All questions carry equal marks**

- 1.a) State and prove Gauss's law.
b) Using the Gauss's law in differential form, obtain the 'E' and 'D' at different points due to the following charge distribution in spherical coordinates.

$$\rho(r, \theta, \phi) = \begin{cases} \rho_0(r/a) & 0 < r < a \\ 0 & a < r < \infty \end{cases} \quad [15]$$

- 2.a) Find the electric field intensity 'E' at a point due to an electric dipole.
b) Find the general equation of flux lines which represent the field $\mathbf{E} = (\mathbf{P}/4\pi\epsilon_0 r^3) (2\cos\theta \mathbf{1}_r + \sin\theta \mathbf{1}_\theta)$ in the spherical coordinate system, when 'P' is a dipole moment. [15]

- 3.a) Define flux density 'D' and explain how electric charge and electric flux is calculated from 'D'.
b) Calculate the 'D' at a point A (6, 4, -5) caused by (i) a point charge of 20mC at the origin. (ii) a uniform line charge density $\rho_l = 20\mu\text{C}/\text{m}$ on the z-axis. (iii) A uniform charge density $\rho_s = 60\mu\text{C}/\text{m}^2$ at a plane $x = 4$. [15]

- 4.a) A Potential field in free space is given by $\mathbf{V} = 60\sin\theta/r^2$. Find the electric flux density 'D' and volume charge density at the point $(\mathbf{r} = 3\mathbf{m}, \theta = 60^\circ, \phi = 25^\circ)$ in spherical coordinates.
b) Calculate the capacitance between two concentric metal spheres of radius ' r_1 ' and ' r_2 ' with charge 'Q' placed on the outer surface of inner shell. [15]

- 5.a) A boundary exists at $z=0$ between two dielectrics $\epsilon r_1 = 2.5$ region $z < 0$ and the $\epsilon r_2 = 4$ region $z > 0$. The Electric field intensity in region $Z < 0$ is $\mathbf{E} = -30\mathbf{1}_x + 50\mathbf{1}_y + 70\mathbf{1}_z \text{ V/m}$. Find (i) E_{n1} (ii) E_{t1} (iii) D_{n2} (iv) D_{t2} (v) D_2 (vi) The angle ' α_1 ' between E_1 and normal to the Surface (vii) Polarization in $Z > 0$ region (viii) The angle ' α_2 ' between D_2 and normal to the surface.
b) A dielectric slab of thickness 'd' with a Non-uniform susceptibility given by $\lambda\epsilon(\mathbf{z}) = \mathbf{z}/(4-\mathbf{z})$ occupies region $1 < \mathbf{z} < 2$. A uniform field $\mathbf{E}_a = E_0 \mathbf{1}_z$ is applied. Calculate the surface charge densities and volume charge density due to polarization. [15]

- 6.a) A circular loop of wire of radius 'a', lying in the "x-y" plane with its centre at the origin carries current 'I' in the + ϕ direction. Using Biot-Savart's law, find $\mathbf{H}(0, 0, z)$ and $\mathbf{H}(0, 0, 0)$.
b) Find the current distribution which produces the field, using Ampere's circuital law in differential form in cylindrical coordinates for the given value of 'H'

$$\mathbf{H} = \begin{cases} J_0 r^2 \mathbf{1}_\phi & 0 < r < a \\ J_0 (a^3/r) \mathbf{1}_\phi & a < r < b \\ 0 & b < r < \infty \end{cases} \quad [15]$$

- 7.a) A variable loop consisting of two stationary parallel conductors connected at one end to a voltmeter, and a moving bar at the other end, moving with a uniform velocity ' v ' m/s. The loop is situated in a uniform flux density ' B_1z ' Tesla. Derive an expression for the EMF induced in the loop for $L=10\text{cm}$, $B=0.21z$ Tesla and $V=20\sqrt{y}$ m/s and if $y=2\text{cm}$ at $t=0$, find for $t=0.006\text{s}$ (i) The ' V ' of the moving bar (ii) ' y ' of the moving bar (iii) The EMF induced in the loop and its polarity.
- b) Verify that the displacement current in the capacitor is same as that of the conduction current in wires. [15]
- 8.a) Derive the Boundary relations in magnetic fields.
- b) A flux density $B=0.05x_1y$ tesla exists in a material having magnetic susceptibility $\lambda_m=2.5$. Find (i) Magnetic field intensity 'H' (ii) Magnetization 'M' (iii) Current Density 'J' (iv) Volume current density due to Magnetization. [15]

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